# ANALYSIS OF TAPER WIDTH VARIATIONS IN LINEAR RELUCTANCE MACHINE

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#### **Abstract**

Linear motors are being used in different application with a huge popularity in the use of transport industry. With the invention of maglev trains and other high speed trains, linear motors are being used for the translation and braking applications for these systems. However, a huge drawback for the linear motor design is the cogging force, low thrust values, and voltage ripples. This paper aims to study the force analysis with change in taper/teeth width of the motor stator and mover to understand the best teeth ratio to obtain a high flux density and a high thrust. The analysis is conducted through JMAG software and it is found that the optimum teeth ratio for both the stator and mover gives an increase of 94.4% increases compared to the 0.5 mm stator and mover width.

Keywords: Force, Linear reluctance motor, Taper, Teeth.

## 1. Introduction

Electric motors are devices that convert the electrical energy to magnetic energy and ultimately into mechanical energy. Electromagnetism is the basis of motor operation in order to produce the magnetic forces required for production of rotational or linear motion [1]. As one of the fastest growing industries, electrical motor manufacturing represents a major industry worldwide, where electric motor driven systems account for approximately 45% of total global electricity consumption and is expected to rise to 13,360 terawatt hour (TWh) by 2030 [2].

Recent developments in the industry have brought forth linear machines that provides mechanical translation without intermediate gears, screws or crankshafts. In a linear motor either the moving or stationary member must extend over the entire range of motion of the moving member [3]. The motion occurs because of the electromagnetic force developed in the actuator. All types of motor configurations and topologies can be produced in the linear fashion, i.e., dc, induction, synchronous and reluctance [4]. Linear electric machines are associated with long linear progressive motion, such as transportation and other similar applications.

The most prominent application of linear motors is the utilization of these motors in transport systems, specifically railway system in the use of train thrust and in braking [5]. Linear reluctance motors are popularly used in electrodynamic braking of high speed trains. These brakes operate on the principle of converting the traction motors of the train to a generator that convert the kinetic energy of the train into electrical power [6].

To overcome the problem of adhesion between the wheel tread and the rail, the braking force in electromagnetic brakes are achieved through strong magnetic forces that are induced with large electromagnets attached to the vehicle over the top of the rails [7]. In Electromagnetic rail brakes, the frictional forces are produced between the electromagnets and the rail [8]. If the electromagnetic fields generate eddy currents in the rails, creating forces acting in the opposite direction of the movement of the train, it is a linear eddy current brake system.

However, these brake systems are still susceptible to the cogging effects of the permanent magnets due to the magnetic retention, which greatly reduces the efficiency of the motor [9]. A linear reluctance motor that does not utilize permanent magnets have been introduced, thus minimizing the cogging force and decreasing the weight of the linear motor. The objective of this paper is to study the different teeth ratios of the linear reluctance motor and to propose a ratio for the best thrust/force characteristic.

## 2. Literature Review

Linear Electric Machines are in general three-phase machines fed through power electronic controllers and taking advantage of regenerative electric braking for fast, robust, and precise thrust, speed, or position control. The topology of a linear switched reluctance motor is similar to that of a stepping motor with variable reluctance platen. In addition, it is equipped with position sensors [10]. The turn-on and turn-off instant of the input current is synchronized with the position of the moving part. The thrust is very sensitive to the turn-on and turn-off instant. In these type of motors, the rotor tends to move to a position where the inductance of the excited winding is maximized or the reluctance is minimized.

In the case of a linear stepping or linear switched reluctance motor, the speed  $\nu$  of the moving part is as in Eq. (1).

$$v = v_s = f_{sw}\tau \tag{1}$$

where  $f_{sw}$  is the fundamental switching frequency in one armature phase winding and  $\tau$  is the pole pitch of the reaction rail. For a rotary stepping or switched reluctance motor  $f_{sw}=2p_rn$  where  $2p_r$  is the number of rotor poles and n is rotational speed in rev/s. The fundamental energy conversion equation for linear electric machines is as in Eq. (2).

$$F\dot{x} = v\dot{i} \tag{2}$$

where F is mechanical force (N),  $\dot{x}$  is mechanical velocity (m/s), v is the Voltage (V), and  $\dot{i}$  is current (A). It is assumed that F and  $\dot{x}$  are in the same direction. Numerous studies have been conducted into increasing the thrust of these linear motors such as [11], where slots are used to decrease harmonic components of the thrust force. These slots can be in the form of skewed or fractional slot [12]. This allows the analysis of rated performance calculation and effects such as cogging torque, ripple torque, back-emf form prediction. Analysis which combines the orthogonal optimization algorithm for tooth shifting and pole shifting of a double-sided slotted permanent magnet synchronous linear motor are carried out in [13].

This study achieves a model with a suppressed thrust ripple which in turn increased the efficiency. A 9-pole 10-slot structure of a short primary permanent magnet LSM is proposed in Bataar et al. [14], which is focused on reducing the cogging force through detent force minimization by optimizing the length of armature core and shape of the exterior teeth simultaneously by using (1+lambda) evolution strategy coupled with response surface method using multi-quadric radial basis function.

Other studies are focused on establishing a platform for the analysis and test of characteristics such as thrust ripples and detent force of the permanent magnet linear motor [15]. It is predicted that thrust ripples are generated by the distortion of the stator flux linkage distribution, reluctance force due to the relative position between the mover and stator, Zhu et al [16], aims to rectify this through the utilization of predictive control algorithm, which will result in the minimization of the voltage ripple by high precision control. The same result is obtained through moving node techniques in research conducted by Lim et al. [17].

Linear Motor Systems which has electromechanical multi-parameter, and strong coupling is difficult to control. Ai et al. [18] proposed an analysis of relative weights of various factors for thrust fluctuations in permanent magnet LM, using the fuzzy analytic hierarchy process to reduce these fluctuations in the thrust. It can be seen through these research that the cogging force deteriorates the performance and even excite the mechanical resonance thus decreasing the efficiency and also the life span of the motor [19]. This paper will look into the teeth size variation for obtaining the highest force in the mover and the stator of the linear motor [20]. The paper will first outline the method of analysis and then propose the results of the study, finally discussing the results and propose a ratio for the best stator and mover teeth gap for a linear reluctance motor based on the results of the study.

# 3. Methodology

The main structure of the linear reluctance motor studied in this paper consists of three basic structures; the stator, which is the stationary non-moving part, the mover, which consists the coil and is the linear translation component. Figure 1 shows the arrangement of the structure.

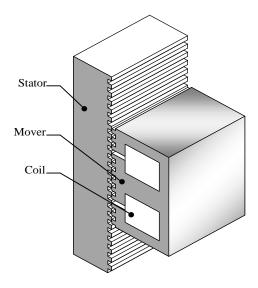


Fig. 1. Linear reluctance motor.

The parameter that is to be studied is the teeth gap of both the stator and mover to show which is the best ratio of teeth width gap for obtaining the highest thrust from the linear motor. Figure 2 shows the parameter to be studied while Figure 3 gives an in depth analysis for obtaining the ratio.

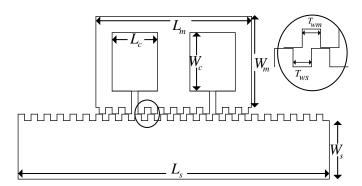


Fig. 2. Parameter to be studied.

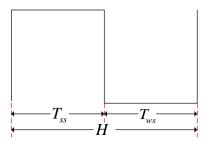


Fig. 3. Teeth ratio.

As seen from Fig. 3, the total pole width of the motor is to be kept constant at 4 mm therefore, the teeth gap for the stator is denoted in Eq. (3).

$$H_s = T_{ss} + T_{ws} \tag{3}$$

where,  $H_s$  is the total width of the pole and  $T_{ss}$  is the gap where the tooth protrudes and  $T_{ws}$  is the dip in the teeth. The parameter  $T_{ws}$  is then changed while keeping  $H_s$  constant.

The same parameter for the mover teeth are also varied to obtain the best ratio for the teeth and the combination of the ratio of the teeth in both stator and mover to obtain the highest thrust. The dimensions of the stator and mover are summarized in Table 1.

The simulations are run on FEM software JMAG. The parameters used for the coil is 330 turns with a total resistance of  $4.6\Omega$ . The material, and circuit parameters are kept constant for the whole analysis. A total of 49 simulations are carried out with different combinations of  $T_{ws}$  and  $T_{wm}$ .

Parameter	Symbol	Value	SI units
Length of stator	$L_s$	96	mm
Width of stator	$W_{s}$	18	mm
Teeth height of stator		2	mm
Length of mover	$L_m$	48	mm
Width of mover	$W_m$	28	mm
Teeth height of mover		2	mm
Length of coil	$L_c$	14	mm
Width of coil	$W_c$	18	mm
Number of turns in coil		330	
Resistance of coil		96	mm

Table 1. List of parameters.

## 4. Results and Discussion

The analysis was run using JMAG software, in order to obtain the flux lines, magnetic flux density, absolute force of translations and other parameters. For this study the force in Y direction of the motor is considered, since increase in the force shows the decrease in cogging force, which shows an increase in the efficiency of motor.

As seen from Fig. 4, an increase in the teeth width of both the stator and the mover, increases the absolute force to a certain point, however further increase shows a decrease in the force that is generated. This can be seen in all of the stator teeth width measurements from  $0.5T_{ws}$  to  $3.5T_{ws}$ . The force in Y direction of  $0.5T_{ws}$  increases from 24 N to 63 N at  $2.5T_{ws}$  and then decreases to 52 N at  $3.5T_{ws}$ . This effect is better illustrated in Fig. 5.

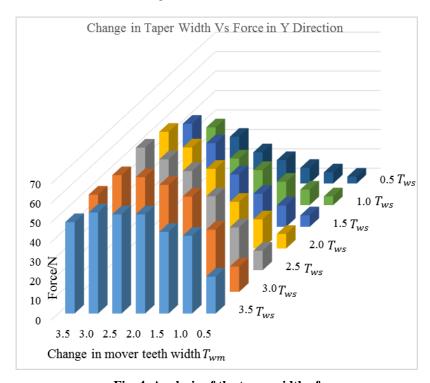


Fig. 4. Analysis of the taper width of stator and mover based on absolute force.

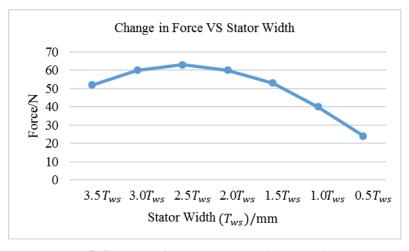


Fig. 5. Change in force with change in teeth width.

As seen the force increases with an increase in the teeth gap showing that that the magnetic flux density increases. This is because as the teeth gap  $T_{ws}$  increases the, extruded part of the teeth which is the  $T_{ss}$  decreases, since total teeth width  $H_s$  is kept constant. This decrease in  $T_{ss}$  decreases the surface area of extrusion, thus forcing the magnetic flux to be concentrated, increasing the density and hence increasing the force. However, a further increase of the gap from  $3.0T_{ws}$  decreases the force since the extruded part of the teeth  $T_{ss}$ , is too small and the magnetic flux leaks from the teeth gap as shown from Fig. 6. This leakage decreases the density of the magnetic flux thus decreasing the force of the motor.

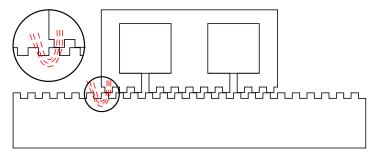


Fig. 6. Leakage of magnetic flux.

The same effect can be seen for the mover teeth width  $T_{wm}$ , for which the force increases from 47 N at 3.5  $T_{wm}$  to 52 N at 3.0  $T_{wm}$  and then decreases to 19 N at 0.5 $T_{wm}$  at a constant stator teeth width of 3.5  $T_{ws}$ . Based on these results it is best to identify which ratio of teeth width for both the stator and the mover provides the highest force, thus increasing the efficiency of the motor. The highest force obtained for each stator width is illustrated in Fig. 7.

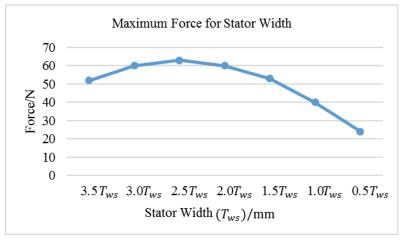


Fig. 7. Maximum force for each stator width.

As shown by the curve in Fig. 7, the highest absolute force for the motor design is at 463 N, which is achieved at  $2.5T_{ws}$ . The graph also shows that the best teeth width for the mover is at  $3.0 T_{wm}$ , since all of the maximum force for the stator is achieved at this teeth width. However, motor design should also take into

consideration the manufacturing process and the materials required. The 2.5 mm teeth width is better since this will decrease the material costs for the motor production. The flux density for this size is also the best since there the distribution is more uniform and the motor shows areas of lower flux concentration which shows that continuous operation of the motor will not result in excessive heat buildup in the body which will result in a lower life span for the motor. The comparison of the flux density for the motor is shown in Fig. 8.

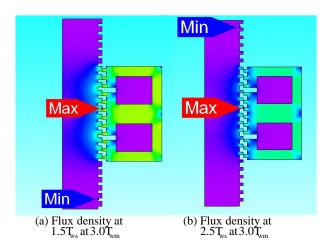


Fig. 8. Flux distribution for 1.5  $T_{ws}$  and 2.5  $T_{ws}$ .

Based on these results it can be seen that the best stator tooth width is 2.5 mm for  $T_{ws}$  and the mover teeth width is 3 mm for  $T_{wm}$ . Both of these ratios provide an increase in 94.4% force compared to 0.5 mm for both the stator and mover, and a 25.4% increase compared to 3.5 mm teeth width for both the stator and mover.

## 5. Conclusions

Linear motors are used for different applications and is gaining popularity in the transport industry mainly in railway systems. The main disadvantage of the current motor types is the cogging force by the use of permanent magnets, and voltage ripple which decreases the thrust force of the linear motor. This study aims to analyse the effects of the linear reluctance motor's taper width of both the stator and mover to identify the best ratio of teeth gap to obtain the highest force values.

The analysis was done through the software JMAG, by changing the parameters of the teeth gap while keeping the other parameters such as motor dimensions, materials, circuit, coil resistance and number of turns constant. The teeth gap of stator  $T_{ws}$  and mover  $T_{wm}$  is changed to obtain the results.

As seen from the analysis the best results for the teeth gap can be found at  $2.5T_{ws}$  and  $3.0 T_{wm}$  which gives an increase of in 94.4% force compared to 0.5 mm for both which is the lowest teeth width that both the stator and mover can achieve.

Further analysis and studies can be conducted by changing the teeth shape and obtaining the optimum teeth shape for increased thrust, decrease in cogging force, and higher efficiency.

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Nomenclatures		
F	Mechanical force	
$f_{sw}$	Switching frequency	
$H_s$	Total width of pole	
n	Rotational speed	
$p_r$	No. of rotor poles	
$T_{ss}$	Tooth protrusion gap	
$T_{ws}$	Tooth dip gap	
v	Speed	
$\dot{x}$	Mechanical velocity	
Greek Symbols		
τ	Pole pitch	
Abbrev	iations	
emf	Electro motive force	
PM	Permanent Magnet	

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